

# ON HOMOMORPHISMS OF EXTENDED-ORDER ALGEBRAS

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The talk will consider the concept of (*weak*) *extended-order algebra* (*w-eo algebra*) introduced by C. Guido [2] (in the wake of *implicative algebras* of H. Rasiowa [3]) as a triple  $(L, \rightarrow, \top)$ , where  $L$  is a set,  $\top$  is a fixed element of  $L$  and  $\rightarrow$  is a binary operation defined on  $L$  satisfying the following conditions: (1)  $a \rightarrow \top = \top$ ; (2)  $a \rightarrow a = \top$ ; (3) if  $a \rightarrow b = \top$  and  $b \rightarrow a = \top$ , then  $a = b$ ; (4) if  $a \rightarrow b = \top$  and  $b \rightarrow c = \top$ , then  $a \rightarrow c = \top$  (in one word, letting  $a \leq b$  iff  $a \rightarrow b = \top$ , gives a partial order on  $L$ ). While H. Rasiowa was interested in providing a common framework for the algebraic structures used in non-classical logics, C. Guido was inspired by those of many-valued mathematics. In particular, he investigated thoroughly the possibility of obtaining all the standard logical connectives (conjunction, disjunction, negation, *etc.*) and their properties (associativity, commutativity, distributivity, *etc.*) from the single one  $\rightarrow$  and its properties, using the technique of adjunctions (also known as Galois connections) for partially ordered sets [1]. The attention of C. Guido and his collaborators, however, was restricted entirely to w-eo algebras, leaving the case of their homomorphisms aside. It is the purpose of the current talk to fill in the gap and provide a detailed description of different kinds of w-eo algebra homomorphisms and their essential properties.

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## REFERENCES

- [1] G. Gierz, K. H. Hofmann, and *etc.*, *Continuous Lattices and Domains*, Cambridge University Press, 2003.
- [2] C. Guido and P. Toto, *Extended-order algebras*, *J. Appl. Log.* **6** (2008), no. 4, 609–626.
- [3] H. Rasiowa, *An Algebraic Approach to Non-Classical Logics*, *Studies in Logics and the Foundations of Mathematics*, vol. 78, North-Holland, Amsterdam, 1974.

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