



# Introduction to Computer Systems

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Systems

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# Question 1a

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- Add the decimal integers 15 and 27
- Show your working

	2	7
+	1, carry	5
Answer:	4	2



# Question 1b

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- Subtract the binary number 101 from the binary number 11001.
- Show your working.

	1	1	borrow, 0	0	1
-		repay	1	0	1
Answer:	1	0	1	0	0



# Question 1c

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- Write out the binary representation of  $2^6 + 2^4$
- $2^6$  is 1000000
- $2^4$  is 10000
- Adding:  $1000000 + 10000 = 1010000$



# Question 1d

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- Explain how the binary representation of a number specifies that number as a sum of powers of 2
- The  $i$ th place in the representation, reading right to left is associated with  $2^{i-1}$ .
- The number is the sum of powers  $2^{i-1}$  for which the digit in the  $i$ th place is 1



# Question 2a

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- Which of the following are Boolean statements?
  - $(3+7)*2$
  - $(3+7) == 2$
  - $C = 4$
  - $6 < 10$
- Answer: those that have a value True or False



# Question 2b

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- Write out the truth table for A OR B.

A	B	A OR B
0	0	0
1	0	1
0	1	1
1	1	1

- Truth tables for NOT A, A AND B, A XOR B?



# Question 2c

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- Write out a Boolean expression that is true if  $x$  is strictly less than  $y$  or strictly greater than  $y+5$
- $x < y$  OR  $x > y+5$





# Question 3a

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- Obtain the Brookshear floating point representation of  $3+(1/4)$
- Recall  $\pm 2^r * 0.t$
- Recall sign bit, exponent and mantissa
- +11.01



# Question 3b

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- What feature allows representations of very large and very small numbers near to 0?
- Recall  $\pm 2^r * 0.t$



# Question 4a

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- Explain the terms track and sector for a hard drive
- Why do the tracks have their shape?



# Question 4b

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- A hard drive has a capacity of 4 TB. The data rate for reading is 100 MB per s.
- How many seconds are required for reading the whole disk?
  
- 0.1 GB per s
- 1 GB in 10 s
- 1 TB = 1000 GB
- 4 TB = 4000 GB read in  $4000 \times 10 = 40000$  s



# Question 5a

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- Give an example of a two-dimensional array of integers.
- Answer: a 3x3 array:

4	1	0
0	4	0
2	3	2



## Question 5b

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- How is it possible to store a 2 dimensional array in a one dimensional memory?
- Answer: one row at a time:

4	1	0
0	4	0
2	3	2

4	1	0	0	4	0	2	3	2
---	---	---	---	---	---	---	---	---



## Question 5c

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- Write a pseudo code algorithm to add the numbers in a one dimensional array  $A$  and print the result.
- Other tasks: max, min, find  $i$  such that
$$A[i] < A[i+1]$$



## Question 5c Continued

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- `sum = 0`
- `i = 0`
- `while i < length(A)`
  - `sum = sum+A[i]`
  - `i = i+1`
- `endWhile`
- `print(sum)`





## Question 6a

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- Explain the action of the instruction with op code 8

Answer: 8RST, bitwise And the contents of registers S and T. Put the result in register R. E.g.

S	0	1	1	0	0	1	1	1
T	0	0	1	1	1	1	1	0
R	0	0	1	0	0	1	1	0



## Question 6b

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- Write a program to load the contents of memory cell 91 into a register, set the rightmost 4 bits to 0 and store the resulting bit string in cell 92.
- Answer:

1191	Load register 1 with the bit pattern in cell 91
22F0	Load register 2 with F0 = 11110000
8312	And registers 1 and 2, put result in register 3
3392	Store the register 3 bit pattern in cell 92



# Question 7a

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- Define the term algorithm. Why are algorithms important?
- Answer (bookwork): an ordered set of unambiguous executable steps that defines a terminating process.
- An algorithm is required for any task to be performed by a computer.



# Question 7b

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- Why is there no algorithm for printing all the integers less than 5?
- Answer: the process requires an infinite number of steps



## Question 7c

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- Implement a loop in a program. Write out a pseudo code example.
- Answer: in a while loop a Boolean expression is evaluated. If the expression is true, then a block of code is executed and the expression is evaluated again. If false, then the code following the while loop is executed



## Question 7c (Example)

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- Pseudo code example of a while loop
- `i = 0`
- `while i < 5`
- `print(i)`
- `i = i+1`
- `endWhile`



## Question 8a

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- Describe one advantage and one disadvantage of a linked list.
- Answer (bookwork): the different items in the list can be stored anywhere in memory
- To access an element it is necessary to search the list item by item



## Question 8b

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- Describe the way in which the head pointer and the null pointer are used.
- Answer (bookwork): the value of the head pointer is the location of the first element on the list.
- The null pointer marks the end of the list.





## Question 8c

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- Replace the item B in the list with the item D

addresses	10	11	12	13	14	15	16	17	18	19
contents	H	12	A	16	C	0	B	14	D	0

initial

H	12	→	A	16	→	B	14	→	C	0
---	----	---	---	----	---	---	----	---	---	---

updated

H	12	→	A	18	→	D	14	→	C	0
---	----	---	---	----	---	---	----	---	---	---



## Question 9a

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- Why is a sequential file appropriate for storing music?
- Answer: when the music is played the records in the file are accessed in the same order that they are stored in the file. This makes access efficient.



## Question 9b

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- Describe the structure of an index file.
- Answer (bookwork): The data in the file is stored in a list of records. Each record is identified by a unique key. The file contains an index which consists of pairs  $(k, a)$  where  $k$  is the key of a record and  $a$  is the address of the location where the record is stored.



## Question 9c

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- An index file contains at most  $2^6$  records. The file is stored in a memory with  $2^{14}$  cells. What is the maximum size of the index in bits?
- Answer: Each pair  $(k, a)$  requires 6 bits for the key and 14 bits for the address. There are at most  $2^6$  pairs. The maximum size of the index is
$$2^6 \times (6 + 14) = 1280 \text{ bits}$$



## Question 10a

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```
function gcd(m, n)
    while (m ≠ n)
        r = m-n
        m = maximum(n, r)
        n = minimum(n, r)
    endwhile
    return m
endFunction
```

- What happens if gcd is called with  $m > 0$  and  $n = 0$  ?



## Question 10a (Continued)

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```
function gcd1(m, n)
    if n == 0, return m
    endIf
    while (m ≠ n)
        r = m-n
        m = maximum(n, r)
        n = minimum(n, r)
    endwhile
    return m
endFunction
```

- Write out a new function gcd1 that returns the GCD if  $m \geq n > 0$  and returns m if  $m > n = 0$ .



## Question 10b

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```
function gcd2(m1, n1)
    if m1 ≥ n1
        return gcd(m1, n1)
    else
        return gcd(n1, m1)
    endIf
endFunction
```

- Write out a new function gcd2 that returns the GCD if  $m \geq n > 0$  or if  $n > m > 0$ .